

# Temperature Dependence of Densities and Excess Molar Volumes of the Ternary Mixture (1-Butanol + Chloroform + Benzene) and its Binary Constituents (1-Butanol + Chloroform and 1-Butanol + Benzene)

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**Abstract** Densities  $\rho$  of the 1-butanol + chloroform + benzene ternary mixture and the 1-butanol + chloroform and 1-butanol + benzene binaries have been measured at six temperatures (288.15, 293.15, 298.15, 303.15, 308.15, and 313.15) K and atmospheric pressure, using an oscillating U-tube densimeter. From these densities, excess molar volumes ( $V^E$ ) were calculated and fitted to the Redlich–Kister equation for all binary mixtures and to the Nagata and Tamura equation for the ternary system. The Radojković et al. equation has been used to predict excess molar volumes of the ternary mixtures. Also,  $V^E$  data of the binary systems were correlated by the van der Waals (vdW1) and Twu–Coon–Bluck–Tilton (TCBT) mixing rules coupled with the Peng–Robinson–Stryjek–Vera (PRSV) equation of state. The prediction and correlation of  $V^E$  data for the ternary system were performed by the same models.

**Keywords** Benzene · Binary mixtures · 1-Butanol · Chloroform · Cubic EOS mixing rules · Densities · Excess molar volumes · Ternary mixture

## 1 Introduction

The study of thermodynamic properties of binary and ternary mixtures contributes to an understanding of the behavior of different liquids and functional groups. This information is very useful in the design of industrial processes and in the development of theories for the liquid state and predictive methods.

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This article is a continuation of our studies [1–6] of the excess molar volumes,  $V^E$ , for binaries and multicomponent mixtures containing different types of organic solvents widely used in various industries [3,4].

Experimental  $V^E$  data provide better insight into molecular interactions and can be used for testing of various correlation and prediction thermodynamic models, including cubic equations of state (CEOS).

Thus, in the current article, the experimental  $V^E$  results were used to analyze factors influencing molecular interactions and packing phenomena between unlike and like molecules.

In this article experimental measurements of the density of the 1-butanol (1)+chloroform (2)+benzene (3) ternary mixture and the 1-butanol (1)+chloroform (2) and 1-butanol (1)+benzene (3) binary constituents are presented, at temperatures of (288.15, 293.15, 298.15, 303.15, 308.15, and 313.15) K and atmospheric pressure. The density data have been used to calculate excess molar volumes of the mixtures.

For the binary mixtures the  $\rho$  and  $V^E$  literature data cover the following temperatures: 303.15 K [7] for the 1-butanol (1) + chloroform (2) mixture and 293.15 K [8], 298.15 K [9], 303.15 K [10], and 308.15 K [9,11] for the 1-butanol (1) + benzene (3) mixture. Although literature  $V^E$  data were reported at several temperatures for the 1-butanol (1) + benzene (3) system, no values of  $V^E$  have been found for the entire temperature range studied here, especially for the 1-butanol (1) + chloroform (2) mixture. Also, to the best of our knowledge, literature data are not available for the investigated ternary system.

$V^E$ 's of the binary mixtures were fitted using the Redlich–Kister expansion [12], and the ternary data with the Nagata and Tamura [13] equation, while the Radojković et al. [14] equation was used for the prediction of the ternary data. The correlation of the binary data was performed by the PRSV CEOS using the selected mixing rules: (i) the composition-dependent van der Waals one-fluid (vdW1) mixing rules [15] and (ii) the mixing rules that incorporate the excess free energy model  $G^E$  developed by Twu and co-workers (TCBT) [16]. The prediction of  $V^E$  of the ternary system was performed by the same vdW1 and TCBT models. For correlation of  $V^E$  of the ternary data, only TCBT mixing rules were used.

## 2 Experimental

### 2.1 Materials

1-Butanol (Merck) was supplied with a purity >99.5 mass% (p.a.), chloroform (stabilized with amylene) by Riedel-de Haen with a purity of 99.8 mass%, while benzene by Aldrich with a purity of 99.9 mass% (HPLC). Table 1 lists the measured densities

**Table 1** Densities  $\rho$  of the pure components at 298.15 K and atmospheric pressure

Component	$\rho(\text{g} \cdot \text{cm}^{-3})$	
	Experimental	Literature
1-Butanol	0.805762	0.80575 [17]
Chloroform	1.479148	1.47970 [17], 1.47919 [18]
Benzene	0.873582	0.87360 [17]

of the pure components at 298.15, and they agree within  $\pm 4 \times 10^{-5} \text{ g} \cdot \text{cm}^{-3}$  with most of the corresponding literature values [17, 18].

## 2.2 Measurements

The density of the mixtures and the corresponding pure substances was measured with an Anton Paar Model DMA 5000 digital vibrating U-tube densimeter, provided with automatic viscosity correction, having a stated accuracy of  $\pm 5 \times 10^{-6} \text{ g} \cdot \text{cm}^{-3}$ . The temperature in the cell was regulated to  $\pm 0.001 \text{ K}$  with a built-in solid-state thermostat. The temperature in the cell was measured by means of two integrated Pt 100 platinum thermometers, and the stability was better than  $\pm 0.002 \text{ K}$ . The reliability of the apparatus was verified daily with dry air and distilled freshly degassed water. To minimize the errors in composition, all mixtures were prepared by mass using the cell and the procedure described previously [19, 20] and a Mettler AG 204 balance with a precision of  $1 \times 10^{-4} \text{ g}$ . The uncertainty of the mole fraction calculation was less than  $\pm 1 \times 10^{-4}$ . All molar quantities were based on the IUPAC relative atomic mass table. The experimental uncertainty in density is about  $\pm 1 \times 10^{-5} \text{ g} \cdot \text{cm}^{-3}$ , while the average uncertainty in the excess molar volume is estimated to be less than  $3 \times 10^{-3} \text{ cm}^3 \cdot \text{mol}^{-1}$ .

## 3 Results and Discussion

### 3.1 Excess Molar Volumes

The excess molar volumes  $V^E$  were calculated from the equation,

$$V^E = \sum_{i=1}^n x_i M_i [(1/\rho) - (1/\rho_i)] \quad (1)$$

where  $n$  is the number of components;  $x_i$  is the mole fraction of component  $i$  in the mixture while  $M_i$  is its molar mass;  $\rho$  and  $\rho_i$  are the measured densities of the mixture and pure component  $i$ , respectively.

Tables 2 and 3 list the measured densities  $\rho$  and the corresponding values of  $V^E$  for the 1-butanol (1)+chloroform (2) and 1-butanol (1)+benzene (3) binary systems as well as for the 1-butanol (1)+chloroform (2)+benzene (3) ternary system. The experimental results for the chloroform (2)+benzene (3) binary system have been presented in our previous paper [4].

Data for the binary mixtures were fitted to a Redlich–Kister [12] (RK) polynomial of the type,

$$V_{ij}^E = x_i x_j \sum_{p=0}^k A_p (2x_i - 1)^p \quad (2)$$

**Table 2** Experimental densities  $\rho$  and excess molar volumes  $V^E$  for the 1-butanol+chloroform and 1-butanol + benzene binary systems, at  $T=(288.15\text{--}313.15)\text{ K}$  and atmospheric pressure

$x_1$	$\rho$ ( $\text{g} \cdot \text{cm}^{-3}$ )	$V^E$ ( $\text{cm}^3 \cdot \text{mol}^{-1}$ )	$x_1$	$\rho$ ( $\text{g} \cdot \text{cm}^{-3}$ )	$V^E$ ( $\text{cm}^3 \cdot \text{mol}^{-1}$ )	$x_1$	$\rho$ ( $\text{g} \cdot \text{cm}^{-3}$ )	$V^E$ ( $\text{cm}^3 \cdot \text{mol}^{-1}$ )
<i>I-Butanol (1) + chloroform (2)</i>								
<i>T = 288.15 K</i>								
0.0000	1.498077	0.0000	0.3474	1.238343	0.0432	0.7008	1.001030	-0.1334
0.0493	1.458967	0.0428	0.4003	1.201440	0.0163	0.7485	0.970420	-0.1414
0.0994	1.420117	0.0696	0.4610	1.159744	-0.0166	0.7987	0.938452	-0.1352
0.1499	1.381858	0.0777	0.4993	1.133810	-0.0406	0.8495	0.906492	-0.1256
0.2003	1.344302	0.0806	0.5517	1.098600	-0.0661	0.8953	0.877854	-0.0982
0.2476	1.309654	0.0759	0.5989	1.067377	-0.0904	0.9475	0.845530	-0.0551
0.2790	1.286969	0.0684	0.6510	1.033234	-0.1118	1.0000	0.813373	0.0000
<i>T = 293.15 K</i>								
0.0000	1.488638	0.0000	0.3474	1.231070	0.0593	0.7008	0.995760	-0.1209
0.0493	1.449824	0.0477	0.4003	1.194482	0.0330	0.7485	0.965404	-0.1308
0.0994	1.411277	0.0788	0.4610	1.153143	0.0001	0.7987	0.933697	-0.1268
0.1499	1.373340	0.0894	0.4993	1.127428	-0.0239	0.8495	0.901999	-0.1203
0.2003	1.336110	0.0940	0.5517	1.092600	-0.0496	0.8953	0.873588	-0.0953
0.2476	1.301761	0.0906	0.5989	1.061553	-0.0749	0.9475	0.841510	-0.0547
0.2790	1.279278	0.0834	0.6510	1.027696	-0.0976	1.0000	0.809573	0.0000
<i>T = 298.15 K</i>								
0.0000	1.479148	0.0000	0.3474	1.223746	0.0771	0.7008	0.990450	-0.1063
0.0493	1.440633	0.0528	0.4003	1.187479	0.0511	0.7485	0.960349	-0.1181
0.0994	1.402389	0.0883	0.4610	1.146500	0.0182	0.7987	0.928907	-0.1166
0.1499	1.364771	0.1019	0.4993	1.121002	-0.0057	0.8495	0.897472	-0.1130
0.2003	1.327863	0.1086	0.5517	1.086400	-0.0318	0.8953	0.869292	-0.0908
0.2476	1.293819	0.1064	0.5989	1.055688	-0.0577	0.9475	0.837462	-0.0526
0.2790	1.271534	0.0998	0.6510	1.022116	-0.0815	1.0000	0.805762	0.0000
<i>T = 303.15 K</i>								
0.0000	1.469612	0.0000	0.3474	1.216374	0.0957	0.7008	0.985097	-0.0906
0.0493	1.431398	0.0578	0.4003	1.180425	0.0704	0.7485	0.955255	-0.1047
0.0994	1.393449	0.0984	0.4610	1.139809	0.0373	0.7987	0.924082	-0.1059
0.1499	1.356152	0.1150	0.4993	1.114527	0.0138	0.8495	0.892910	-0.1052
0.2003	1.319568	0.1238	0.5517	1.080300	-0.0130	0.8953	0.864961	-0.0856
0.2476	1.285822	0.1233	0.5989	1.049776	-0.0393	0.9475	0.833386	-0.0506
0.2790	1.263746	0.1168	0.6510	1.016495	-0.0645	1.0000	0.801923	0.0000
<i>T = 308.15 K</i>								
0.0000	1.460025	0.0000	0.3474	1.208943	0.1157	0.7008	0.979698	-0.0739
0.0493	1.422115	0.0628	0.4003	1.173313	0.0910	0.7485	0.950115	-0.0901
0.0994	1.384450	0.1094	0.4610	1.133064	0.0577	0.7987	0.919208	-0.0937
0.1499	1.347474	0.1291	0.4993	1.107999	0.0345	0.8495	0.888303	-0.0961
0.2003	1.311210	0.1404	0.5517	1.074000	0.0074	0.8953	0.860590	-0.0797
0.2476	1.277767	0.1413	0.5989	1.043814	-0.0196	0.9475	0.829272	-0.0479
0.2790	1.255896	0.1352	0.6510	1.010818	-0.0456	1.0000	0.798053	0.0000
<i>T = 313.15 K</i>								
0.0000	1.450413	0.0000	0.3474	1.201478	0.1361	0.7008	0.974260	-0.0568
0.0493	1.412816	0.0674	0.4003	1.166161	0.1125	0.7485	0.944940	-0.0755
0.0994	1.375410	0.1214	0.4610	1.126294	0.0777	0.7987	0.914297	-0.0813
0.1499	1.338756	0.1441	0.4993	1.101418	0.0570	0.8495	0.883670	-0.0881
0.2003	1.302801	0.1586	0.5517	1.067800	0.0273	0.8953	0.856188	-0.0743
0.2476	1.269664	0.1608	0.5989	1.037803	0.0015	0.9475	0.825138	-0.0471
0.2790	1.248018	0.1536	0.6510	1.005107	-0.0267	1.0000	0.794147	0.0000
<i>I-Butanol (1) + benzene (3)</i>								
<i>T = 288.15 K</i>								
0.0000	0.884246	0.0000	0.2997	0.860741	0.1863	0.7010	0.833239	0.0938

**Table 2** continued

$x_1$	$\rho$ (g · cm <sup>-3</sup> )	$V^E$ (cm <sup>3</sup> · mol <sup>-1</sup> )	$x_1$	$\rho$ (g · cm <sup>-3</sup> )	$V^E$ (cm <sup>3</sup> · mol <sup>-1</sup> )	$x_1$	$\rho$ (g · cm <sup>-3</sup> )	$V^E$ (cm <sup>3</sup> · mol <sup>-1</sup> )
0.0193	0.882483	0.0353	0.3532	0.856936	0.1846	0.7502	0.829979	0.0749
0.0534	0.879595	0.0758	0.4019	0.853504	0.1809	0.7945	0.827051	0.0579
0.1013	0.875720	0.1157	0.4525	0.850000	0.1716	0.8511	0.823296	0.0389
0.1509	0.871829	0.1462	0.4998	0.846738	0.1625	0.8961	0.820299	0.0260
0.2016	0.867984	0.1654	0.5532	0.843129	0.1455	0.9510	0.816663	0.0091
0.2018	0.867955	0.1669	0.6004	0.839985	0.1265	1.0000	0.813373	0.0000
0.2500	0.864382	0.1780	0.6493	0.836693	0.1115			
<i>T = 293.15 K</i>								
0.0000	0.878918	0.0000	0.2997	0.855806	0.1984	0.7010	0.828949	0.1016
0.0193	0.877168	0.0377	0.3532	0.852081	0.1972	0.7502	0.825772	0.0813
0.0534	0.874309	0.0815	0.4019	0.848721	0.1939	0.7945	0.822920	0.0629
0.1013	0.870495	0.1237	0.4525	0.845300	0.1840	0.8511	0.819258	0.0424
0.1509	0.866677	0.1555	0.4998	0.842111	0.1748	0.8961	0.816336	0.0282
0.2016	0.862908	0.1756	0.5532	0.838594	0.1565	0.9510	0.812791	0.0096
0.2018	0.862874	0.1777	0.6004	0.835529	0.1365	1.0000	0.809573	0.0000
0.2500	0.859372	0.1896	0.6493	0.832317	0.1205			
<i>T = 298.15 K</i>								
0.0000	0.873582	0.0000	0.2997	0.850849	0.2120	0.7010	0.824631	0.1114
0.0193	0.871844	0.0402	0.3532	0.847201	0.2116	0.7502	0.821537	0.0898
0.0534	0.869007	0.0881	0.4019	0.843914	0.2086	0.7945	0.818759	0.0701
0.1013	0.865255	0.1326	0.4525	0.840574	0.1984	0.8511	0.815196	0.0475
0.1509	0.861506	0.1660	0.4998	0.837460	0.1889	0.8961	0.812348	0.0320
0.2016	0.857807	0.1876	0.5532	0.834030	0.1697	0.9510	0.808897	0.0113
0.2018	0.857776	0.1894	0.6004	0.831042	0.1488	1.0000	0.805762	0.0000
0.2500	0.854344	0.2023	0.6493	0.827910	0.1320			
<i>T = 303.15 K</i>								
0.0000	0.868233	0.0000	0.2997	0.845866	0.2268	0.7010	0.820282	0.1223
0.0193	0.866507	0.0428	0.3532	0.842294	0.2272	0.7502	0.817269	0.0993
0.0534	0.863694	0.0945	0.4019	0.839080	0.2245	0.7945	0.814569	0.0779
0.1013	0.859995	0.1422	0.4525	0.835817	0.2142	0.8511	0.811102	0.0533
0.1509	0.856309	0.1778	0.4998	0.832778	0.2042	0.8961	0.808331	0.0361
0.2016	0.852685	0.2004	0.5532	0.829436	0.1841	0.9510	0.804977	0.0129
0.2018	0.852651	0.2026	0.6004	0.826525	0.1622	1.0000	0.801923	0.0000
0.2500	0.849285	0.2167	0.6493	0.823473	0.1443			
<i>T = 308.15 K</i>								
0.0000	0.862871	0.0000	0.2997	0.840854	0.2430	0.7010	0.815895	0.1346
0.0193	0.861158	0.0452	0.3532	0.837357	0.2442	0.7502	0.812965	0.1100
0.0534	0.858360	0.1019	0.4019	0.834214	0.2418	0.7945	0.810343	0.0867
0.1013	0.854713	0.1528	0.4525	0.831029	0.2313	0.8511	0.806975	0.0596
0.1509	0.851089	0.1907	0.4998	0.828059	0.2214	0.8961	0.804274	0.0415
0.2016	0.847536	0.2145	0.5532	0.824804	0.2002	0.9510	0.801025	0.0147
0.2018	0.847499	0.2170	0.6004	0.821974	0.1769	1.0000	0.798053	0.0000
0.2500	0.844201	0.2322	0.6493	0.819001	0.1580			
<i>T = 313.15 K</i>								
0.0000	0.857498	0.0000	0.2997	0.835830	0.2587	0.7010	0.811483	0.1466
0.0193	0.855809	0.0465	0.3532	0.832400	0.2615	0.7502	0.808640	0.1199
0.0534	0.853019	0.1088	0.4019	0.829324	0.2597	0.7945	0.806094	0.0946
0.1013	0.849433	0.1619	0.4525	0.826217	0.2488	0.8511	0.802822	0.0653
0.1509	0.845861	0.2030	0.4998	0.823320	0.2385	0.8961	0.800189	0.0463
0.2016	0.842375	0.2283	0.5532	0.820157	0.2155	0.9510	0.797051	0.0151
0.2018	0.842342	0.2305	0.6004	0.817402	0.1912	1.0000	0.794147	0.0000
0.2500	0.839110	0.2468	0.6493	0.814449	0.1778			

**Table 3** Experimental densities  $\rho$  and excess molar volumes  $V^E$  for the 1-butanol (1) + chloroform (2) + benzene (3) ternary system at  $T = (288.15\text{--}313.15)\text{ K}$  and atmospheric pressure

$x_1$	$x_2$	$\rho$ (g · cm $^{-3}$ )	$V^E$ (cm $^3$ · mol $^{-1}$ )	$x_1$	$x_2$	$\rho$ (g · cm $^{-3}$ )	$V^E$ (cm $^3$ · mol $^{-1}$ )
<i>T</i> = 288.15 K							
0.0906	0.0999	0.931435	0.1738	0.5389	0.1010	0.899497	0.1145
0.0787	0.2010	0.989208	0.2135	0.4856	0.1974	0.956866	0.1359
0.0698	0.2996	1.046683	0.2336	0.4200	0.2995	1.019836	0.1492
0.0591	0.4023	1.108113	0.2377	0.3606	0.4006	1.083361	0.1538
0.0547	0.4980	1.166249	0.2289	0.3000	0.4971	1.145811	0.1552
0.0405	0.5972	1.228764	0.2122	0.2388	0.5967	1.211706	0.1546
0.0294	0.6816	1.282824	0.2016	0.1801	0.6987	1.280679	0.1487
0.0203	0.7851	1.351079	0.1311	0.1207	0.7997	1.351169	0.1209
0.1793	0.0999	0.924387	0.2138	0.0615	0.8957	1.420354	0.0837
0.1712	0.1977	0.979833	0.2437	0.7128	0.1020	0.888415	0.0144
0.1417	0.3001	1.040893	0.2593	0.6404	0.2010	0.948600	0.0082
0.1197	0.3995	1.101288	0.2499	0.5584	0.2992	1.010178	0.0314
0.1001	0.5004	1.163756	0.2353	0.4790	0.4004	1.074927	0.0493
0.0793	0.5994	1.226676	0.2127	0.3993	0.4995	1.139982	0.0727
0.0588	0.7018	1.293355	0.1745	0.3206	0.5992	1.206986	0.0913
0.0433	0.7983	1.357306	0.1367	0.2393	0.6997	1.276532	0.1087
0.0186	0.9020	1.428941	0.0739	0.1605	0.7998	1.347822	0.0992
0.3607	0.0993	0.910702	0.2050	0.0809	0.8963	1.418925	0.0791
0.3199	0.2003	0.970092	0.2271	0.8111	0.0999	0.881131	-0.0822
0.2776	0.3061	1.033855	0.2362	0.7185	0.1999	0.942900	-0.0636
0.2384	0.3991	1.091477	0.2324	0.6289	0.2991	1.005673	-0.0556
0.1979	0.5010	1.155872	0.2256	0.5411	0.3998	1.070364	-0.0161
0.1587	0.5980	1.218808	0.2062	0.4498	0.5004	1.137082	0.0122
0.1217	0.6993	1.286139	0.1653	0.3579	0.6015	1.205629	0.0594
0.0803	0.7980	1.353781	0.1284	0.2669	0.6985	1.273712	0.0798
0.0410	0.8957	1.422419	0.0811	0.1791	0.7991	1.345658	0.0964
<i>T</i> = 293.15 K							
0.0906	0.0999	0.925887	0.1778	0.5389	0.1010	0.894582	0.1296
0.0787	0.2010	0.983315	0.2141	0.4856	0.1974	0.951609	0.1455
0.0698	0.2996	1.040436	0.2320	0.4200	0.2995	1.014123	0.1585
0.0591	0.4023	1.101474	0.2346	0.3606	0.4006	1.077169	0.1639
0.0547	0.4980	1.159228	0.2256	0.3000	0.4971	1.139140	0.1650
0.0405	0.5972	1.221313	0.2085	0.2388	0.5967	1.204553	0.1616
0.0294	0.6816	1.275166	0.1867	0.1801	0.6987	1.272941	0.1579
0.0203	0.7851	1.342752	0.1284	0.1207	0.7997	1.342891	0.1273
0.1793	0.0999	0.918970	0.1778	0.0615	0.8957	1.411506	0.0887
0.1712	0.1977	0.974084	0.2482	0.7128	0.1020	0.883840	0.0218
0.1417	0.3001	1.034746	0.2614	0.6404	0.2010	0.943582	0.0179
0.1197	0.3995	1.094734	0.2510	0.5584	0.2992	1.004682	0.0429
0.1001	0.5004	1.156780	0.2354	0.4790	0.4004	1.068925	0.0619
0.0793	0.5994	1.219254	0.2127	0.3993	0.4995	1.133454	0.0861
0.0588	0.7018	1.285446	0.1748	0.3206	0.5992	1.199949	0.1019
0.0433	0.7983	1.348934	0.1370	0.2393	0.6997	1.268877	0.1213
0.0186	0.9020	1.420062	0.0720	0.1605	0.7998	1.339580	0.1095
0.3607	0.0993	0.905562	0.2148	0.0809	0.8963	1.410088	0.0863
0.3199	0.2003	0.964564	0.2349	0.8111	0.0999	0.876597	-0.0636
0.2776	0.3061	1.027894	0.2427	0.7185	0.1999	0.938013	-0.0543
0.2384	0.3991	1.085106	0.2383	0.6289	0.2991	1.000288	-0.0435
0.1979	0.5010	1.149034	0.2311	0.5411	0.3998	1.064458	-0.0020
0.1587	0.5980	1.211497	0.2117	0.4498	0.5004	1.130614	0.0282
0.1217	0.6993	1.278317	0.1706	0.3579	0.6015	1.198647	0.0710

**Table 3** continued

$x_1$	$x_2$	$\rho$ (g · cm $^{-3}$ )	$V^E$ (cm $^3$ · mol $^{-1}$ )	$x_1$	$x_2$	$\rho$ (g · cm $^{-3}$ )	$V^E$ (cm $^3$ · mol $^{-1}$ )
0.0803	0.7980	1.345434	0.1330	0.2669	0.6985	1.266105	0.0936
0.0410	0.8957	1.413555	0.0837	0.1791	0.7991	1.337448	0.1079
<i>T = 298.15 K</i>							
0.0906	0.0999	0.920323	0.1823	0.5389	0.1010	0.889639	0.1465
0.0787	0.2010	0.977401	0.2154	0.4856	0.1974	0.946317	0.1571
0.0698	0.2996	1.034161	0.2314	0.4200	0.2995	1.008370	0.1698
0.0591	0.4023	1.094806	0.2321	0.3606	0.4006	1.070941	0.1752
0.0547	0.4980	1.152171	0.2230	0.3000	0.4971	1.132428	0.1761
0.0405	0.5972	1.213828	0.2050	0.2388	0.5967	1.197330	0.1716
0.0294	0.6816	1.267429	0.1744	0.1801	0.6987	1.265158	0.1680
0.0203	0.7851	1.334382	0.1259	0.1207	0.7997	1.334546	0.1356
0.1793	0.0999	0.913529	0.2285	0.0615	0.8957	1.402612	0.0939
0.1712	0.1977	0.968308	0.2539	0.7128	0.1020	0.879232	0.0314
0.1417	0.3001	1.028567	0.2647	0.6404	0.2010	0.938529	0.0295
0.1197	0.3995	1.088148	0.2530	0.5584	0.2992	0.999147	0.0563
0.1001	0.5004	1.149765	0.2366	0.4790	0.4004	1.062876	0.0767
0.0793	0.5994	1.211791	0.2135	0.3993	0.4995	1.126878	0.1013
0.0588	0.7018	1.277502	0.1751	0.3206	0.5992	1.192843	0.1154
0.0433	0.7983	1.340520	0.1374	0.2393	0.6997	1.261173	0.1350
0.0186	0.9020	1.411118	0.0713	0.1605	0.7998	1.331279	0.1212
0.3607	0.0993	0.900395	0.2262	0.0809	0.8963	1.401202	0.0939
0.3199	0.2003	0.959004	0.2444	0.8111	0.0999	0.872028	-0.0423
0.2776	0.3061	1.021894	0.2510	0.7185	0.1999	0.933090	-0.0430
0.2384	0.3991	1.078697	0.2456	0.6289	0.2991	0.994861	-0.0292
0.1979	0.5010	1.142154	0.2379	0.5411	0.3998	1.058510	0.0139
0.1587	0.5980	1.204145	0.2180	0.4498	0.5004	1.124115	0.0448
0.1217	0.6993	1.270448	0.1769	0.3579	0.6015	1.191589	0.0861
0.0803	0.7980	1.337037	0.1385	0.2669	0.6985	1.258449	0.1086
0.0410	0.8957	1.404643	0.0865	0.1791	0.7991	1.329180	0.1207
<i>T = 303.15 K</i>							
0.0906	0.0999	0.914732	0.1879	0.5389	0.1010	0.884667	0.1641
0.0787	0.2010	0.971460	0.2174	0.4856	0.1974	0.940990	0.1697
0.0698	0.2996	1.027856	0.2314	0.4200	0.2995	1.002577	0.1823
0.0591	0.4023	1.088107	0.2299	0.3606	0.4006	1.064666	0.1880
0.0547	0.4980	1.145079	0.2209	0.3000	0.4971	1.125667	0.1886
0.0405	0.5972	1.206307	0.2018	0.2388	0.5967	1.190050	0.1834
0.0294	0.6816	1.259585	0.1668	0.1801	0.6987	1.257328	0.1789
0.0203	0.7851	1.325972	0.1235	0.1207	0.7997	1.326143	0.1450
0.1793	0.0999	0.908057	0.2379	0.0615	0.8957	1.393672	0.0993
0.1712	0.1977	0.962500	0.2606	0.7128	0.1020	0.874591	0.0418
0.1417	0.3001	1.022349	0.2694	0.6404	0.2010	0.933435	0.0424
0.1197	0.3995	1.081525	0.2559	0.5584	0.2992	0.993567	0.0712
0.1001	0.5004	1.142715	0.2382	0.4790	0.4004	1.056782	0.0927
0.0793	0.5994	1.204292	0.2145	0.3993	0.4995	1.120257	0.1176
0.0588	0.7018	1.269511	0.1762	0.3206	0.5992	1.185676	0.1309
0.0433	0.7983	1.332062	0.1382	0.2393	0.6997	1.253417	0.1498
0.0186	0.9020	1.402114	0.0715	0.1605	0.7998	1.322923	0.1339
0.3607	0.0993	0.895193	0.2392	0.0809	0.8963	1.392267	0.1020
0.3199	0.2003	0.953408	0.2552	0.8111	0.0999	0.867437	-0.0214
0.2776	0.3061	1.015857	0.2604	0.7185	0.1999	0.928130	-0.0308
0.2384	0.3991	1.072249	0.2539	0.6289	0.2991	0.989396	-0.0141
0.1979	0.5010	1.135231	0.2458	0.5411	0.3998	1.052519	0.0309
0.1587	0.5980	1.196748	0.2253	0.4498	0.5004	1.117570	0.0624

**Table 3** continued

$x_1$	$x_2$	$\rho$ (g · cm $^{-3}$ )	$V^E$ (cm $^3$ · mol $^{-1}$ )	$x_1$	$x_2$	$\rho$ (g · cm $^{-3}$ )	$V^E$ (cm $^3$ · mol $^{-1}$ )
0.1217	0.6993	1.262540	0.1835	0.3579	0.6015	1.184465	0.1035
0.0803	0.7980	1.328606	0.1436	0.2669	0.6985	1.250742	0.1246
0.0410	0.8957	1.395692	0.0892	0.1791	0.7991	1.320855	0.1347
<i>T = 308.15 K</i>							
0.0906	0.0999	0.909117	0.1942	0.5389	0.1010	0.879675	0.1814
0.0787	0.2010	0.965493	0.2199	0.4856	0.1974	0.935620	0.1838
0.0698	0.2996	1.021520	0.2320	0.4200	0.2995	0.996737	0.1964
0.0591	0.4023	1.081372	0.2285	0.3606	0.4006	1.058343	0.2022
0.0547	0.4980	1.137945	0.2197	0.3000	0.4971	1.118863	0.2019
0.0405	0.5972	1.198745	0.1991	0.2388	0.5967	1.182714	0.1966
0.0294	0.6816	1.251642	0.1631	0.1801	0.6987	1.249442	0.1910
0.0203	0.7851	1.317514	0.1215	0.1207	0.7997	1.317691	0.1550
0.1793	0.0999	0.902557	0.2484	0.0615	0.8957	1.384679	0.1051
0.1712	0.1977	0.956662	0.2683	0.7128	0.1020	0.869909	0.0534
0.1417	0.3001	1.016091	0.2755	0.6404	0.2010	0.928301	0.0563
0.1197	0.3995	1.074857	0.2603	0.5584	0.2992	0.987945	0.0871
0.1001	0.5004	1.135626	0.2404	0.4790	0.4004	1.050635	0.1104
0.0793	0.5994	1.196753	0.2160	0.3993	0.4995	1.113580	0.1355
0.0588	0.7018	1.261470	0.1781	0.3206	0.5992	1.178458	0.1474
0.0433	0.7983	1.323565	0.1388	0.2393	0.6997	1.245604	0.1659
0.0186	0.9020	1.393049	0.0726	0.1605	0.7998	1.314511	0.1476
0.3607	0.0993	0.889956	0.2536	0.0809	0.8963	1.383274	0.1109
0.3199	0.2003	0.947777	0.2670	0.8111	0.0999	0.862844	-0.0032
0.2776	0.3061	1.009777	0.2713	0.7185	0.1999	0.923125	-0.0174
0.2384	0.3991	1.065755	0.2636	0.6289	0.2991	0.983881	0.0025
0.1979	0.5010	1.128264	0.2545	0.5411	0.3998	1.046476	0.0493
0.1587	0.5980	1.189307	0.2333	0.4498	0.5004	1.110971	0.0814
0.1217	0.6993	1.254576	0.1913	0.3579	0.6015	1.177285	0.1222
0.0803	0.7980	1.320130	0.1490	0.2669	0.6985	1.242979	0.1417
0.0410	0.8957	1.386690	0.0921	0.1791	0.7991	1.312472	0.1497
<i>T = 313.15 K</i>							
0.0906	0.0999	0.903502	0.1992	0.5389	0.1010	0.874675	0.1969
0.0787	0.2010	0.959515	0.2220	0.4856	0.1974	0.930242	0.1962
0.0698	0.2996	1.015161	0.2332	0.4200	0.2995	0.990878	0.2099
0.0591	0.4023	1.074634	0.2259	0.3606	0.4006	1.052000	0.2159
0.0547	0.4980	1.130771	0.2200	0.3000	0.4971	1.112032	0.2153
0.0405	0.5972	1.191159	0.1966	0.2388	0.5967	1.175356	0.2096
0.0294	0.6816	1.243655	0.1609	0.1801	0.6987	1.241530	0.2032
0.0203	0.7851	1.309028	0.1198	0.1207	0.7997	1.309220	0.1646
0.1793	0.0999	0.897040	0.2590	0.0615	0.8957	1.375665	0.1108
0.1712	0.1977	0.950816	0.2750	0.7128	0.1020	0.865196	0.0652
0.1417	0.3001	1.009798	0.2831	0.6404	0.2010	0.923143	0.0696
0.1197	0.3995	1.068159	0.2655	0.5584	0.2992	0.982294	0.1028
0.1001	0.5004	1.128523	0.2421	0.4790	0.4004	1.044466	0.1274
0.0793	0.5994	1.189204	0.2166	0.3993	0.4995	1.106856	0.1549
0.0588	0.7018	1.253412	0.1797	0.3206	0.5992	1.171241	0.1618
0.0433	0.7983	1.315067	0.1380	0.2393	0.6997	1.237743	0.1834
0.0186	0.9020	1.383942	0.0747	0.1605	0.7998	1.306053	0.1627
0.3607	0.0993	0.884700	0.2679	0.0809	0.8963	1.374240	0.1208
0.3199	0.2003	0.942119	0.2794	0.8111	0.0999	0.858299	0.0064
0.2776	0.3061	1.003675	0.2821	0.7185	0.1999	0.918097	-0.0049
0.2384	0.3991	1.059428	0.2575	0.6289	0.2991	0.978341	0.0184
0.1979	0.5010	1.121270	0.2636	0.5411	0.3998	1.040403	0.0676

**Table 3** continued

$x_1$	$x_2$	$\rho$ (g · cm <sup>-3</sup> )	$V^E$ (cm <sup>3</sup> · mol <sup>-1</sup> )	$x_1$	$x_2$	$\rho$ (g · cm <sup>-3</sup> )	$V^E$ (cm <sup>3</sup> · mol <sup>-1</sup> )
0.1587	0.5980	1.181862	0.2398	0.4498	0.5004	1.104344	0.1003
0.1217	0.6993	1.246591	0.1989	0.3579	0.6015	1.170087	0.1402
0.0803	0.7980	1.311632	0.1543	0.2669	0.6985	1.235174	0.1599
0.0410	0.8957	1.377672	0.0946	0.1791	0.7991	1.304056	0.1652

**Table 4** Parameters  $A_p$  of Eq. 2 and the corresponding  $\sigma$  for the binary mixtures

$T$ (K)	$A_0$	$A_1$	$A_2$	$A_3$	$\sigma$ (cm <sup>3</sup> · mol <sup>-1</sup> )
<i>I-Butanol (1) + chloroform (2)</i>					
288.15	-0.1560	-1.1307	-0.0291	-0.0178	0.0024
293.15	-0.0893	-1.1449	-0.0304	-0.0563	0.0023
298.15	-0.0162	-1.1487	-0.0234	-0.0999	0.0023
303.15	0.0616	-1.1487	-0.0036	-0.1630	0.0023
308.15	0.1429	-1.1688	0.0071	-0.1847	0.0022
313.15	0.2277	-1.1652	0.0147	-0.2317	0.0037
<i>I-Butanol (1) + benzene (3)</i>					
288.15	0.6370	-0.5121	0.1825	-0.1858	0.0027
293.15	0.6827	-0.5362	0.1967	-0.2141	0.0031
298.15	0.7429	-0.5456	0.1876	-0.2473	0.0035
303.15	0.8026	-0.5673	0.2010	-0.2891	0.0038
308.15	0.8636	-0.5964	0.2457	-0.2946	0.0041
313.15	0.9346	-0.5902	0.2435	-0.3799	0.0044

where  $A_p$  denotes the adjustable parameters and  $k+1$  is their number determined by means of the  $F$ -test [21].

Adjustable parameters of the fits at each temperature separately and the corresponding root-mean-square deviations (rmsd),  $\sigma$ , defined by the equation,

$$\sigma = \left( \sum_{i=1}^m (V_{\text{exp},i}^E - V_{\text{cal},i}^E)^2 / m \right)^{1/2} \quad (3)$$

are given in Table 4. In Eq. 3,  $m$  is the number of experimental data points.

The ternary  $V^E$ 's were predicted using the Radojković et al. [14] equation;

$$V_{123}^E = V_{12}^E + V_{13}^E + V_{23}^E \quad (4)$$

where  $V_{12}^E$ ,  $V_{13}^E$ , and  $V_{23}^E$  represent the binary excess molar volumes calculated by Eq. 2, while  $x_1$ ,  $x_2$ , and  $x_3$  are the mole fractions of the ternary system.

The ternary  $V^E$  were correlated by the Nagata and Tamura [13] model;

$$V_{123}^E = V_{12}^E + V_{13}^E + V_{23}^E + x_1 x_2 x_3 RT (B_0 - B_1 x_1 - B_2 x_2 - B_3 x_1^2 - B_4 x_2^2 - B_5 x_1 x_2 - B_6 x_1^3 - B_7 x_2^3 - B_8 x_1^2 x_2) \quad (5)$$

where  $B_0, B_1, \dots, B_8$  are the adjustable parameters of the ternary contribution obtained from the ternary experimental  $V^E$  data. These fitted parameters of Eq. 5 along with the corresponding  $\sigma$  for Eqs. 4 and 5, calculated according to Eq. 3, are given in Table 5.

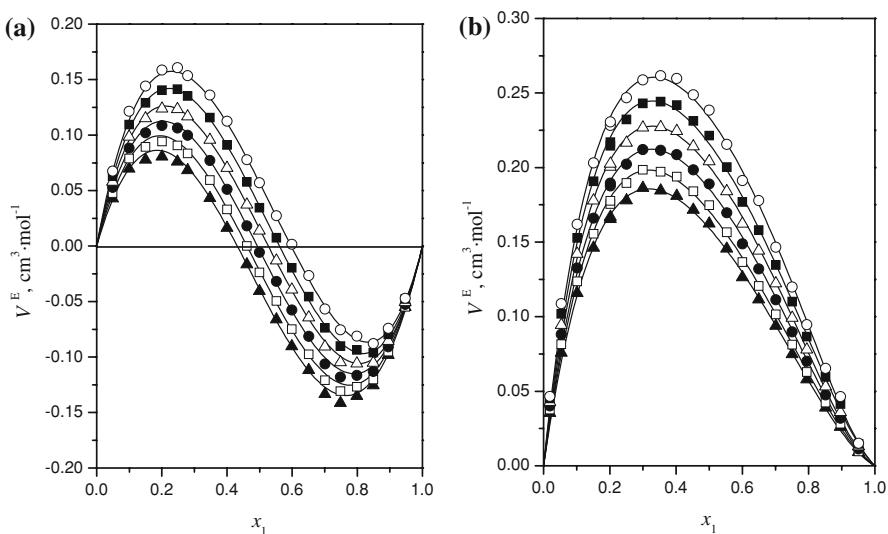
In Fig. 1a, b the experimental  $V^E$  data for the 1-butanol (1)+chloroform (2) and 1-butanol (1)+benzene (3) binary systems were plotted for the following investigated temperatures: (288.15, 293.15, 298.15, 303.15, 308.15, and 313.15) K. As can be seen from Fig. 1a, the 1-butanol (1)+chloroform (2) system exhibits an S-shape of the  $V^E - x_1$  curves (maximum with positive and minimum with negative values of  $V^E$ ), with  $V^E$  values increasing with temperature from 288.15 K to 313.15 K. As can be seen from Fig. 1b, the 1-butanol (1)+benzene (3) system shows positive  $V^E$  values over the whole concentration range, also with  $V^E$  values increasing with increasing temperature. Comparisons of our experimental results of  $V^E$  for the 1-butanol (1)+benzene (3) system at (293.15, 298.15, 303.15, and 308.15) K with the data reported previously [8–10] show that our  $V^E$  data are in very good agreement (for the maximum  $V^E$  values, at  $x_1 = 0.35$ , the difference is less than 4% for all studied temperatures). Larger disagreements exist only for the case of data reported by Bhardwaj et al. [11] at 308.15 K (nearly 15%). Since the 1-butanol (1)+chloroform (2) system exhibits an S-shape of the  $V^E - x_1$  curves, comparisons between the experimental and literature data [7] at 303.15 K were performed in the area of maximum (at  $x_1 = 0.2$ ) and minimum  $V^E$  values (at  $x_1 = 0.8$ ). The maximum experimental  $V^E$  value is higher comparing to the literature (about 10%), while  $V^E$  values for the minimum are in very good agreement (the difference is about 3%).

For the investigated mixtures,  $V^E$  data can be explained qualitatively on the basis of the following resulting opposite contributions that are predominant in a certain mole-fraction region: (i) the positive values in the 1-butanol lower region may be due to the disruptive or stretching effects on the self-associated molecular structure of 1-butanol, (ii) the negative values are thought to be due to the specific interactions between unlike molecules, and (iii) the accommodation of benzene or chloroform in the intermolecular space of the 1-butanol network structure leads to more dense packing and results in the volume reduction that occurs in the region rich in 1-butanol. The magnitude and sign of  $V^E$  have been interpreted as the result of a balance between these effects.

$V^E$ 's of the 1-butanol (1)+chloroform (2) mixture plotted in Fig. 1a exhibit the S-shape form of the  $V^E - x_1$  curves. The positive values in the 1-butanol lower region are a consequence of a rupture of the hydrogen bonding of a self-associated aggregate of 1-butanol and a steric effect between the alkyl chain of the alcohol and the Cl atom of the chloroform. The maximum values of  $V^E$  appear at smaller  $x_1$  where the dissociation of 1-butanol agglomerates is more extensive. On the other hand, the presence of a larger amount of 1-butanol has an effect of changing the positive sign of  $V^E$  to negative, suggesting that a more compact structure is obtained. Namely, chloroform molecules are fitted into a three-dimensional associated 1-butanol network showing that their breaking is not complete. Also, the negative  $V^E$  values arise from changes of free volumes at the real condition and specific interactions between the 1-butanol chain fragment and molecules of chloroform. The disruptive effect of self-associated aggregates of 1-butanol increases with increasing temperature, while the

**Table 5** Parameters  $B_i$  of Eq. 5 and the corresponding  $\sigma$  of the prediction, Eq. 4, and correlation, Eq. 5, for the 1-butanol (1) + chloroform (2) + benzene (3) ternary system

$T$ (K)	288.15	293.15	298.15	303.15	308.15	313.15
Prediction $\sigma(\text{cm}^3 \cdot \text{mol}^{-1})$	0.0289	0.0291	0.0293	0.0297	0.0306	0.0303
Correlation						
$B_0$	$0.1538 \times 10^{-3}$	$0.1928 \times 10^{-3}$	$0.3019 \times 10^{-3}$	$0.4563 \times 10^{-3}$	$0.4875 \times 10^{-3}$	$0.7643 \times 10^{-3}$
$B_1$	$-0.1400 \times 10^{-2}$	$-0.1469 \times 10^{-2}$	$-0.1197 \times 10^{-2}$	$-0.4973 \times 10^{-3}$	$-0.6068 \times 10^{-3}$	$0.8462 \times 10^{-3}$
$B_2$	$-0.4987 \times 10^{-2}$	$-0.4595 \times 10^{-2}$	$-0.4061 \times 10^{-2}$	$-0.3511 \times 10^{-2}$	$-0.3116 \times 10^{-2}$	$-0.2063 \times 10^{-2}$
$B_3$	$0.3263 \times 10^{-3}$	$0.1158 \times 10^{-2}$	$0.1871 \times 10^{-2}$	$0.1417 \times 10^{-2}$	$0.1954 \times 10^{-2}$	$-0.7815 \times 10^{-3}$
$B_4$	$0.8547 \times 10^{-2}$	$0.7256 \times 10^{-2}$	$0.6306 \times 10^{-2}$	$0.5629 \times 10^{-2}$	$0.4220 \times 10^{-2}$	$0.2233 \times 10^{-2}$
$B_5$	$0.1130 \times 10^{-1}$	$0.1088 \times 10^{-1}$	$0.9545 \times 10^{-2}$	$0.7364 \times 10^{-2}$	$0.7620 \times 10^{-2}$	$0.6361 \times 10^{-2}$
$B_6$	$0.4206 \times 10^{-2}$	$0.2605 \times 10^{-2}$	$0.8080 \times 10^{-3}$	$-0.1179 \times 10^{-3}$	$-0.9328 \times 10^{-3}$	$0.7429 \times 10^{-3}$
$B_7$	$-0.5114 \times 10^{-2}$	$-0.3927 \times 10^{-2}$	$-0.3302 \times 10^{-2}$	$-0.2780 \times 10^{-2}$	$-0.1638 \times 10^{-2}$	$-0.2917 \times 10^{-3}$
$B_8$	$-0.1649 \times 10^{-1}$	$-0.1489 \times 10^{-1}$	$-0.1259 \times 10^{-1}$	$-0.8915 \times 10^{-2}$	$-0.8869 \times 10^{-2}$	$-0.7672 \times 10^{-2}$
$\sigma(\text{cm}^3 \cdot \text{mol}^{-1})$	0.0059	0.0044	0.0035	0.0035	0.0040	0.0049

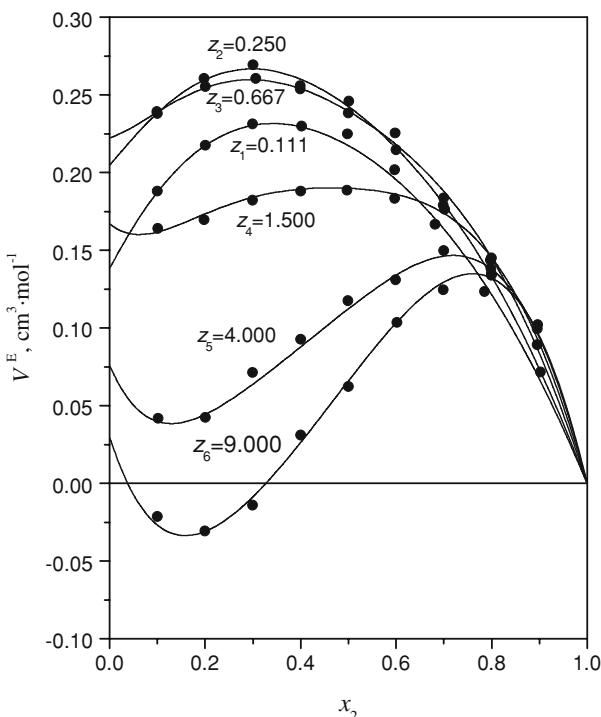


**Fig. 1** Experimental values of  $V^E$  data for (a) 1-butanol (1)+chloroform (2) and (b) 1-butanol (1)+benzene (2). Symbols refer to experimental points at:  $\blacktriangle$  288.15 K;  $\square$  293.15 K;  $\bullet$  298.15 K;  $\triangle$  303.15 K;  $\blacksquare$  308.15 K; and  $\circ$  313.15 K, while the lines represent the results calculated by Eq. 2

number of cross-associated H bonds decreases in the alcohol-rich region causing less negative  $V^E$ .

Table 2 and Fig. 1b show that experimental  $V^E$  data of the 1-butanol (1)+benzene (3) mixture are positive over the whole composition range at all investigated temperatures. These positive values of  $V^E$  can be qualitatively explained by disruptive or stretching effects on the self-associated molecular structure of 1-butanol. The possible formation of weak  $\text{H}\cdots\pi$  bonding between the OH group of 1-butanol and  $\pi$  electrons of the benzene ring has not resulted in negative  $V^E$  values. As suggested by Assarson and Eirich [22], components of similar molecular sizes such as 1-butanol and benzene (vdW volumes of  $52.4 \text{ cm}^3 \cdot \text{mol}^{-1}$  and  $48.4 \text{ cm}^3 \cdot \text{mol}^{-1}$ , respectively) mix with positive values of  $V^E$ . From Table 2 and Fig. 1b, it can be seen that in all cases  $V^E$  of this system increases with increasing temperature. It is clear that a rupture of the hydrogen bonding of self-associated molecules of 1-butanol increases with increasing temperature leading to higher positive  $V^E$  results. The factors that cause changes of  $V^E$  for the chloroform (2)+benzene (3) binary mixture have been described previously [3,4].

Ternary  $V^E$  data can be plotted for lines of constant  $z (= x_1/x_3)$ . Figure 2 shows experimental values of  $V^E$  at 303.15 K and fitted lines of  $z$  obtained by means of Eq. 5. From this figure it is observed that a larger amount of benzene up to  $z_3$  gives expansive values of  $V^E$  which change in a contractive way when adding a large amount of 1-butanol ( $z_5$  and  $z_6$ ) at a lower mole fraction of chloroform. This effect could be attributed to the interaction of 1-butanol and benzene with chloroform. Isolines at constant values of the ternary  $V^E$  at 288.15 K and 315.15 K obtained by Eq. 5 were plotted in Fig. 3a and b, respectively. Positive  $V^E$  values were obtained over most of

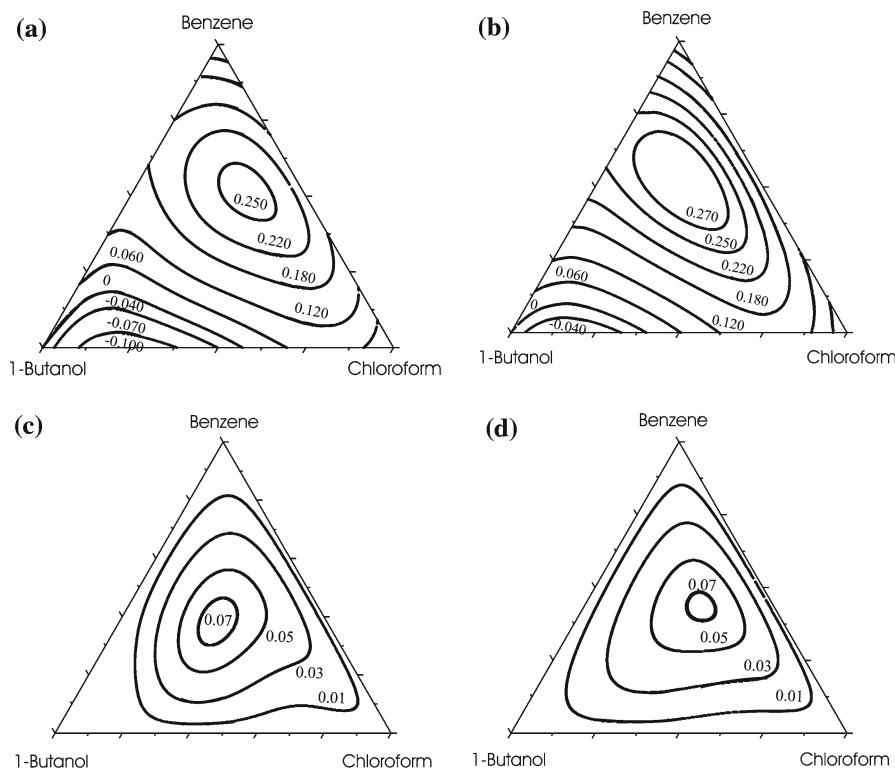


**Fig. 2** Excess molar volumes ( $V^E$ ) for the 1-butanol (1)+chloroform (2)+benzene (3) ternary system, at 303.15 K and atmospheric pressure, along the curves of constant ratio  $z = x_1/x_3$  as a function of the chloroform composition. Symbols represent the experimental points. Solid curves were calculated by Eq. 5

the composition range, except in the region which is close to 1-butanol in the binary mixture with chloroform where the sign is negative. Namely, the latter contractive trend of  $V^E$  shown in Fig. 1a is due to greater packing in this system. This situation could be also confirmed in Fig. 2 as already pointed out for  $z_6 = 9.000$  and in the low region of chloroform at 303.15 K. Maximum values of  $V^E$  appear close to the chloroform (2)+benzene (3) binary mixture suggesting that the unpacking effect, which is the result of complex formation of chloroform (2)+benzene (3) and the disruptive effect on the self-associated molecules of 1-butanol, are more dominant. The increase in temperature, as can be seen from Fig. 3a and b, only confirms this viewpoint.

It is also observed that maximum values of  $V^E$  increase with increasing temperature. As expected, this expansive trend with increasing temperature means that the negative region of  $V^E$  is diminished. As shown in Fig. 3c and d, the ternary contribution  $\Delta V_{123}^E$  is positive and relatively significant with a maximum  $V^E$  located around the center of the triangular diagram at 288.15 K, and shifted toward the chloroform (2)+benzene (3) binary system at 313.15 K.  $\Delta V_{123}^E$  is about 38% at 288.15 K and about 26% at 313.15 K of the total magnitude of  $V_{123}^E$ , respectively.

The three-dimensional surfaces of  $V_{123}^E$  generated from the Nagata and Tamura Eq. 5 at 288.15 K and 313.15 K were plotted in Fig. 4a and b, respectively. The ternary  $V_{123}^E$



**Fig. 3** Curves of constant  $V_{123}^E$  ( $\text{cm}^3 \cdot \text{mol}^{-1}$ ) for the 1-butanol (1) + chloroform (2) + benzene (3) ternary system, at (a) 288.15 K and (b) 313.15 K. Lines represent results calculated by Eq. 5. Curves of ternary contribution  $\Delta V^E$  ( $\text{cm}^3 \cdot \text{mol}^{-1}$ ),  $\Delta V^E = V_{123}^E - V_{12}^E - V_{13}^E - V_{23}^E$ , for the same system at (c) 288.15 K, and (d) 313.15 K. Lines represent results calculated by the ternary contribution of Eq. 5

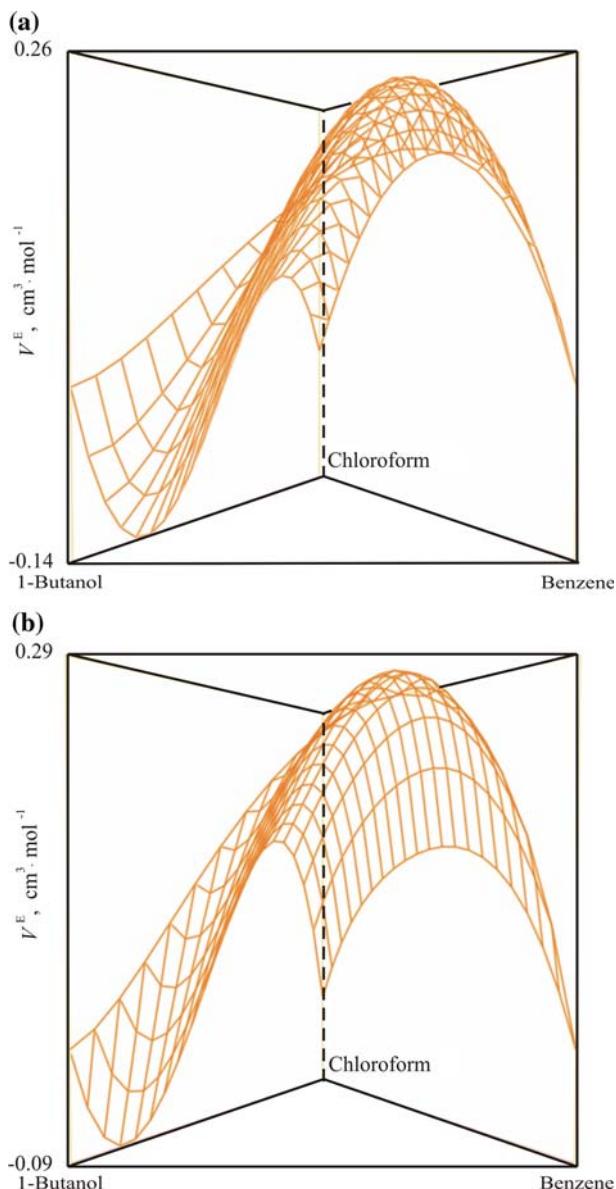
show large positive and small negative values, and they show insignificant changes with increasing temperature.

### 3.2 Cubic EOS Mixing Rules

Stryjek and Vera [23] proposed a two-parameter cubic equation of state (PRSV CEOS) as a modification of the Peng–Robinson equation in the following form:

$$P = \frac{RT}{V - b} - \frac{a}{V(V + b) + b(V - b)} \quad (6)$$

where  $P$ ,  $T$ , and  $V$  are the pressure, temperature, and molar volume, respectively, and  $R$  is the universal gas constant.



**Fig. 4** Three-dimensional surfaces for the 1-butanol (1) + chloroform (2) + benzene (3) ternary system at (a) 288.15 K and (b) 313.15 K, generated by Eq. 5

The temperature-dependent energy  $a_i$  and covolume  $b_i$  are pure component parameters obtained from

$$a_i(T) = 0.457235 \frac{(RT_{ci})^2}{P_{ci}} \left[ 1 + m_i \left( 1 - T_{ri}^{1/2} \right) \right]^2 \quad (7)$$

$$b_i = 0.077796 \frac{RT_{ci}}{P_{ci}} \quad (8)$$

where  $T_{ci}$  and  $P_{ci}$  are the critical temperature and critical pressure of component  $i$ , respectively.

In Eq. 7,  $m$  is a parameter given by

$$m_i = k_{0i} + k_{1i} \left(1 + T_{ri}^{1/2}\right) (0.7 - T_{ri}) \text{ and} \quad (9)$$

$$k_{0i} = 0.378893 + 1.4897153\omega_i - 0.1713848\omega_i^2 + 0.0196554\omega_i^3 \quad (10)$$

where  $T_{ri}$  stands for the reduced temperature ( $T/T_{ci}$ ),  $\omega_i$  is the acentric factor, and  $k_{1i}$  denotes the pure substance adjustable parameter [23].

Two different mixing rules for determining the PRSV CEOS mixing parameters  $a$  and  $b$  were investigated here: vdW1 and TCBT. The vdW1 mixing rule [15] is expressed as

$$a = \sum_i \sum_j x_i x_j (a_i a_j)^{1/2} [1 - k_{ij} + l_{ij} (x_i - x_j)] \quad (11)$$

and

$$b = \sum_i \sum_j x_i x_j (b_i b_j)^{1/2} (1 - m_{ij}) \quad (12)$$

where  $k_{ij}$ ,  $l_{ij}$ , and  $m_{ij}$  are the adjustable binary interaction parameters, estimated for both binary mixtures. Since the TCBT mixing rule [16] has been applied successfully in our previous articles [1–4], it was used here. This mixing rule, developed for no reference pressure conditions and based on the van der Waals reference fluid (vdW), can be represented as

$$\begin{aligned} \frac{G^E}{RT} - \frac{G_{\text{vdW}}^E}{RT} + (Z - Z_{\text{vdW}}) &= \ln \left[ \left( \frac{V_{\text{vdW}}^* - 1}{V^* - 1} \right) \left( \frac{b_{\text{vdW}}}{b} \right) \right] \\ &\quad - \frac{1}{w - u} \left[ \frac{a^*}{b^*} \ln \left( \frac{V^* + w}{V^* + u} \right) \right. \\ &\quad \left. - \frac{a_{\text{vdW}}^*}{b_{\text{vdW}}^*} \ln \left( \frac{V_{\text{vdW}}^* + w}{V_{\text{vdW}}^* + u} \right) \right] \end{aligned} \quad (13)$$

where  $G_{\text{vdW}}^E$  is calculated for the PRSV CEOS. Parameters  $a_{\text{vdW}}$  and  $b_{\text{vdW}}$  were calculated by Eqs. 11 and 12. All reduced parameters  $a^*$ ,  $b^*$ ,  $a_{\text{vdW}}^*$ , and  $b_{\text{vdW}}^*$  are determined as follows:

$$a^* = Pa/R^2T^2 \quad b^* = Pb/RT \quad (14)$$

The reduced volume  $V^* = V/b = Z/b^*$  is defined at  $P$  and  $T$  of the mixture. Equation 6 given in the form for the factor compressibility  $Z$  was used to calculate  $Z$  and  $Z_{\text{vdW}}$ . Bearing in mind that  $V^*$  does not have an explicit solution, an iterative technique was required for the calculation.

The NRTL equation [24] was applied as the  $G^E$  model in Eq. 13 according to the expression,

$$\frac{G^E}{RT} = \sum_i x_i \frac{\sum_j x_j G_{ji} \tau_{ji}}{\sum_k x_k G_{ki}} \quad (15)$$

where for binary mixtures,

$$\begin{aligned} G_{12} &= \exp(-\alpha_{12} \tau_{12}) & G_{21} &= \exp(-\alpha_{12} \tau_{21}) \\ \tau_{12} &= \frac{\Delta g_{12}}{RT} = (g_{12} - g_{22}) / RT & \tau_{21} &= \frac{\Delta g_{21}}{RT} = (g_{21} - g_{11}) / RT \end{aligned} \quad (16)$$

and for a ternary mixture,

$$\tau'_{ij} = \tau_{ij} + \frac{\sum_{k=1}^n x_k \Delta g_{ijk}}{RT} \quad (17)$$

$\Delta g_{12}$  and  $\Delta g_{21}$  are the binary energy parameters and  $\Delta g_{ijk}$  represents the ternary contribution.

The temperature-dependent parameters for the CEOS and CEOS/ $G^E$  models used in the investigated temperature range were obtained as

$$Y = Y_1 + Y_2 T \quad (18)$$

where  $Y = k_{ij}, l_{ij}, m_{ij}, \Delta g_{12}$ , and  $\Delta g_{21}$ . Corresponding models applied here were made by using adequate equations, and they are listed in Table 6. Parameters or coefficients of these models were obtained by minimizing the following objective function:

$$\text{OF} = \frac{1}{m} \sum_{i=1}^m \left( \frac{V_{\text{exp}}^E - V_{\text{cal}}^E}{V_{\text{exp}}^E} \right)_i^2 \rightarrow \min \quad (19)$$

using the Marquardt optimization technique [25].

The obtained results of  $V^E$  calculation were assessed by the percentage average absolute deviation  $\text{PD}(V^E)$

$$\text{PD}(V^E) = \frac{100}{m} \sum_{i=1}^m \left| \frac{V_{\text{exp}}^E - V_{\text{cal}}^E}{(V_{\text{exp}}^E)_{\max}} \right|_i \quad (20)$$

where  $(V_{\text{exp}}^E)_{\max}$  denotes the maximum absolute value of experimental  $V^E$  points.

**Table 6** Coefficients and results of correlation of the  $V^E$  data, given by PD( $V^E$ ) and  $\sigma$ , obtained by the temperature-independent PRSV CEOS models for the investigated binary systems at the temperatures (288.15–313.15) K and atmospheric pressure

$T$ (K)	$k_{ij,1}$	$l_{ij,1}$	$m_{ij,1}$	$\Delta g_{12,1}$ (J · mol $^{-1}$ )	$\Delta g_{21,1}$ (J · mol $^{-1}$ )	PD( $V^E$ ) (%)	$\sigma$ (cm $^3$ · mol $^{-1}$ )
<i>I-Butanol (1) + chloroform (2)</i>							
288.15							
vdW1-2 <sup>a</sup>	0.1181		0.0046			5.02	0.0077
vdW1-3 <sup>b</sup>	0.1612	0.0168	0.0111			1.80	0.0031
TCBT-2 <sup>c</sup>				$-0.227514 \times 10^4$	$0.358796 \times 10^4$	11.95	0.0191
TCBT-3 <sup>d</sup>	-0.1021			$-0.208666 \times 10^4$	$-0.166802 \times 10^4$	1.45	0.0026
293.15							
vdW1-2	0.1163		0.0046			5.51	0.0079
vdW1-3	0.1583	0.0161	0.0112			2.18	0.0036
TCBT-2				$-0.228780 \times 10^4$	$0.359391 \times 10^4$	12.86	0.0190
TCBT-3	-0.1030			$-0.207367 \times 10^4$	$-0.164897 \times 10^4$	1.51	0.0024
298.15							
vdW1-2	0.1140		0.0045			5.94	0.0078
vdW1-3	0.1536	0.0150	0.0109			2.73	0.0040
TCBT-2				$-0.228963 \times 10^4$	$0.357902 \times 10^4$	13.88	0.0187
TCBT-3	-0.1048			$-0.207702 \times 10^4$	$-0.164153 \times 10^4$	1.69	0.0023
303.15							
vdW1-2	0.1117		0.0044			5.53	0.0078
vdW1-3	0.1490	0.0139	0.0106			2.94	0.0044
TCBT-2				$-0.228586 \times 10^4$	$0.355394 \times 10^4$	12.88	0.0184
TCBT-3	-0.1042			$-0.203210 \times 10^4$	$-0.159719 \times 10^4$	1.54	0.0025
308.15							
vdW1-2	0.1094		0.0042			4.67	0.0078
vdW1-3	0.1435	0.0126	0.0101			2.89	0.0049
TCBT-2				$-0.227858 \times 10^4$	$0.352440 \times 10^4$	10.90	0.0180
TCBT-3	-0.1066			$-0.205027 \times 10^4$	$-0.158964 \times 10^4$	1.50	0.0028
313.15							
vdW1-2	0.1064		0.0039			4.63	0.0091
vdW1-3	0.1418	0.0129	0.0103			3.23	0.0064
TCBT-2				$-0.226975 \times 10^4$	$0.349191 \times 10^4$	9.92	0.0185
TCBT-3	-0.1068			$-0.201376 \times 10^4$	$-0.156483 \times 10^4$	1.98	0.0045
288.15–313.15							
vdW1-2	0.1056		0.0033			10.32	0.0162
vdW1-3	0.0788–0.0118–0.0010					8.39	0.0129
TCBT-2				$-0.225785 \times 10^4$	$0.350293 \times 10^4$	15.22	0.0249
TCBT-3	-0.0352			$0.433231 \times 10^4$	$-0.366352 \times 10^4$	6.32	0.0106
<i>I-Butanol (1) + benzene (3)</i>							
288.15							
vdW1-2	0.0725		0.0012			2.15	0.0054
vdW1-3	-0.0101–0.0261–0.0099					1.53	0.0035
TCBT-2				$-0.874348 \times 10^3$	$0.170486 \times 10^4$	1.31	0.0037
TCBT-3	-0.0010			$-0.959123 \times 10^3$	$0.176730 \times 10^4$	1.31	0.0036
293.15							
vdW1-2	0.0734		0.0015			2.21	0.0060
vdW1-3	-0.1147–0.0598–0.0238					1.02	0.0030
TCBT-2				$-0.927679 \times 10^3$	$0.175449 \times 10^4$	1.42	0.0042
TCBT-3	-0.0017			$-0.106730 \times 10^4$	$0.185799 \times 10^4$	1.42	0.0041
298.15							
vdW1-2	0.0738		0.0017			2.32	0.0068

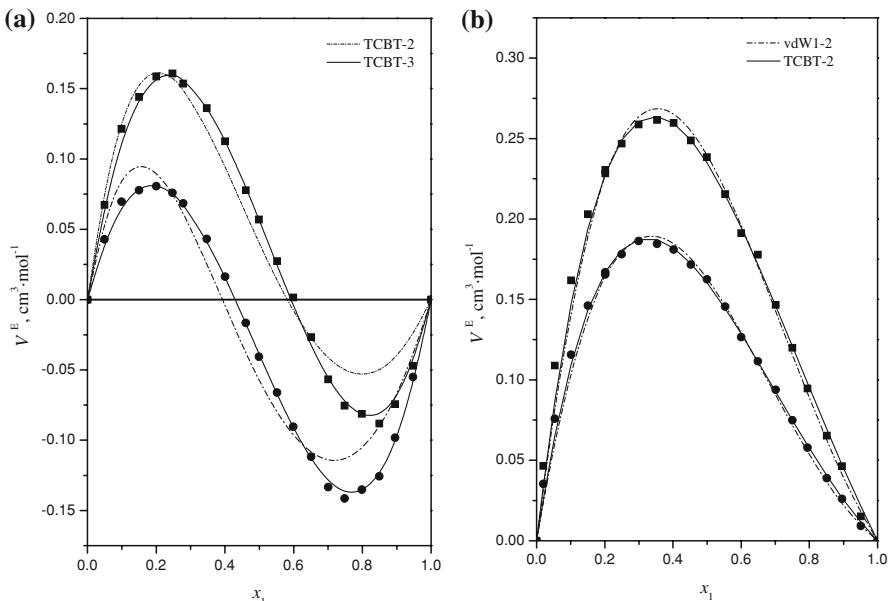
**Table 6** continued

<i>T</i> (K)	<i>k<sub>ij</sub></i> ,1	<i>l<sub>ij</sub></i> ,1	<i>m<sub>ij</sub></i> ,1	$\Delta g_{12,1}$ (J · mol <sup>-1</sup> )	$\Delta g_{21,1}$ (J · mol <sup>-1</sup> )	PD( <i>V</i> <sup>E</sup> ) (%)	$\sigma$ (cm <sup>3</sup> · mol <sup>-1</sup> )
vdW1-3	−0.1097	−0.0572	−0.0239			1.08	0.0035
TCBT-2				$−0.954670 \times 10^3$	$0.176918 \times 10^4$	1.47	0.0050
TCBT-3	−0.0011			$−0.104883 \times 10^4$	$0.184507 \times 10^4$	1.45	0.0048
303.15	vdW1-2	0.0743	0.0020			2.43	0.0076
	vdW1-3	−0.1042	−0.0546	−0.0239		1.15	0.0040
	TCBT-2			$−0.101517 \times 10^4$	$0.183326 \times 10^4$	1.50	0.0053
	TCBT-3	−0.0048		$−0.137346 \times 10^4$	$0.210231 \times 10^4$	1.50	0.0052
	vdW1-2	0.0747	0.0022			2.55	0.0085
308.15	vdW1-3	−0.0978	−0.0518	−0.0238		1.26	0.0046
	TCBT-2			$−0.103397 \times 10^4$	$0.184074 \times 10^4$	1.59	0.0062
	TCBT-3	−0.0058		$−0.150969 \times 10^4$	$0.223456 \times 10^4$	1.58	0.0058
	vdW1-2	0.0747	0.0024			2.66	0.0092
313.15	vdW1-3	−0.1001	−0.0515	−0.0249		1.41	0.0052
	TCBT-2			$−0.105207 \times 10^4$	$0.184635 \times 10^4$	1.77	0.0072
	TCBT-3	−0.0061		$−0.156877 \times 10^4$	$0.229562 \times 10^4$	1.73	0.0063
	vdW1-2	−0.0677	0.0009			4.55	0.0117
288.15–313.15	vdW1-3	0.0423	−0.0096	−0.0029		1.77	0.0056
	TCBT-2			$−0.882690 \times 10^3$	$0.165950 \times 10^4$	10.31	0.0270
	TCBT-3	−0.0287		$0.226899 \times 10^4$	$−0.230477 \times 10^4$	2.76	0.0083

<sup>a</sup> Eqs. 6–12, 18;  $l_{ij} = 0$ <sup>b</sup> Eqs. 6–12, 18<sup>c</sup> Eqs. 6–16, 18;  $k_{ij} = l_{ij} = m_{ij} = 0$ ;  $\alpha_{ij} = 0.3$ <sup>d</sup> Eqs. 6–16, 18;  $l_{ij} = m_{ij} = 0$ ;  $\alpha_{ij} = 0.3$ 

The fitting parameters of the temperature-independent vdW1 and TCBT models, as well as PD(*V*<sup>E</sup>) and  $\sigma$  are shown in Table 6. As can be seen from Table 6, the best agreement with experimental data was achieved by the three-parameter vdW1-3 and TCBT-3 models. The PD(*V*<sup>E</sup>) for the 1-butanol (1) + chloroform (2) system for both models increase with increasing temperature. It means that the 1-butanol (1)+chloroform (2) system with the S-shape of the  $V^E - x_1$  curve is not easy to fit. The temperature-independent vdW1-2 and TCBT-2 models gave relatively large deviations for each separate isotherm, while all models do not work well for the whole temperature range.

A different situation was found for the 1-butanol (1)+benzene (3) binary system where the results obtained with all models are better, particularly those achieved by the vdW1-3 model which is simpler than TCBT-3. The dissimilar fitting of aforementioned systems can be observed in Fig. 5a and b. Figure 5a shows a different quality of the sigmoidal  $V^E - x_1$  fit for the 1-butanol (1)+chloroform (2) system, resulting from the temperature-independent TCBT-2 and TCBT-3 models at 288.15 K and 313.15 K. Namely, the TCBT-2 model fails in the case of maximum and minimum *V*<sup>E</sup> data fitting. Contrarily, as shown in Fig. 5b, the temperature-independent two-parameter vdW1-2 and



**Fig. 5** Correlation of  $V^E$  data for the binary systems: **(a)** 1-butanol (1) + chloroform (2) and **(b)** 1-butanol (1) + benzene (3). Symbols refer to experimental points at: ●, 288.15 K; ■, 298.15 K, while the lines represent the results calculated by PRSV CEOS models

TCBT-2 models gave a similar quality of results, which could be considered as satisfactory. The results obtained over the whole temperature range by temperature-dependent CEOS and CEOS/ $G^E$  models together with their coefficients are listed in Table 7. For the 1-butanol (1)+chloroform (2) system, low PD( $V^E$ ) and  $\sigma$  were obtained only for the TCBT-3 model, and are better than those obtained by the temperature-independent TCBT-3 model (Table 6). For the 1-butanol (1)+benzene (3) mixture, better results for PD( $V^E$ ) and  $\sigma$  calculations were achieved by temperature-dependent TCBT-2 and TCBT-3 models, compared to the vDW1-2 and vDW1-3 models.

Prediction of  $V^E$  for the 1-butanol (1) + chloroform (2) + benzene (3) ternary system at each temperature and over the whole range of temperature, were carried out using the CEOS and CEOS/ $G^E$  models, with binary interaction parameters of these models generated from binary data. The corresponding PD( $V^E$ ) and  $\sigma$  are given in Table 8. It is evident that predictions carried out by the simple vDW1-2 model could be treated as acceptable and similar to those obtained by Radojkovic et al., Eq. 4. The results for other models are poor, except those achieved by the temperature-independent vDW1-3 model for the whole temperature range. Correlation of ternary  $V^E$  data of this system, using only TCBT models was based on the ternary contribution incorporated in Eq. 17. As can be seen from Table 9, better agreement with experimental  $V^E$  data for each temperature and the whole temperature range was obtained with the TCBT-3 model. However, for the whole temperature range, the TCBT-2 model with temperature-dependent parameters works satisfactorily.

**Table 7** Coefficients and results of correlation of the  $V^E$  data, given by PD( $V^E$ ), and  $\sigma$ , obtained by the temperature-dependent PRSV CEOS models for the investigated binary systems over the temperature range (288.15–313.15) K and atmospheric pressure

	$k_{ij,1}$	$l_{ij,1}$	$m_{ij,1}$	$\Delta g_{12,1}(J \cdot mol^{-1})$	$\Delta g_{21,1}(J \cdot mol^{-1})$	PD( $V^E$ )	$\sigma$
	$k_{ij,2}(K^{-1})$	$l_{ij,2}(K^{-1})$	$m_{ij,2}(K^{-1})$	$\Delta g_{12,2}(J \cdot mol^{-1} \cdot K^{-1})$	$\Delta g_{21,2}(J \cdot mol^{-1} \cdot K^{-1})$	(%)	(cm $^3 \cdot mol^{-1}$ )
<i>I-Butanol (1) + chloroform (2)</i>							
vdW1-2 <sup>a</sup>	0.2429		0.0109			5.23	0.0081
	-0.433 $\times 10^{-3}$		-0.218 $\times 10^{-4}$			5.22	0.0082
vdW1-3 <sup>b</sup>	-0.6247	-0.4709	0.0113			12.24	0.0185
	0.119 $\times 10^{-2}$	0.107 $\times 10^{-2}$	-0.199 $\times 10^{-3}$	-0.244877 $\times 10^4$			
TCBT-2 <sup>c</sup>				0.487381 $\times 10^0$	-0.433531 $\times 10^1$		
TCBT-3 <sup>d</sup>	-0.1048			-0.479366 $\times 10^4$	-0.279641 $\times 10^4$	2.90	0.0055
				0.910166 $\times 10^1$	0.388945 $\times 10^1$		
<i>I-Butanol (1) + benzene (3)</i>							
vdW1-2	0.0473		-0.0120			2.39	0.0072
	0.884 $\times 10^{-4}$		0.462 $\times 10^{-4}$				
vdW1-3	4.5371	1.3592	0.6512			4.01	0.0102
	-0.152 $\times 10^{-1}$	-0.464 $\times 10^{-2}$	-0.222 $\times 10^{-2}$	0.535297 $\times 10^3$	0.101258 $\times 10^4$	1.91	0.0058
TCBT-2				-0.518576 $\times 10^1$	0.281591 $\times 10^1$		
TCBT-3	0.0178			0.187177 $\times 10^4$	0.134081 $\times 10^4$	1.90	0.0062
				-0.638858 $\times 10^1$	0.584935 $\times 10^0$		

<sup>a</sup> Eqs. 6–12, 18;  $l_{ij} = 0$

<sup>b</sup> Eqs. 6–12, 18

<sup>c</sup> Eqs. 6–16, 18;  $k_{ij} = l_{ij} = m_{ij} = 0$ ;  $\alpha_{ij} = 0.3$

<sup>d</sup> Eqs. 6–16, 18;  $l_{ij} = m_{ij} = 0$ ;  $\alpha_{ij} = 0.3$

**Table 8** Results of prediction of  $V^E$ , given by  $\text{PD}(V^E)$  and  $\sigma$ , for the 1-butanol (1) + chloroform (2) + benzene (3) ternary system

$T$ (K)	$\text{vdW}1\text{-}2^{\text{a}}$ $\text{PD}(V^E)$ (%)	$\sigma$ ( $\text{cm}^3 \cdot \text{mol}^{-1}$ )	$\text{vdW}1\text{-}3^{\text{b}}$ $\text{PD}(V^E)$ (%)	$\sigma$ ( $\text{cm}^3 \cdot \text{mol}^{-1}$ )	$\text{TCBT-2}^{\text{c}}$ $\text{PD}(V^E)$ (%)	$\sigma$ ( $\text{cm}^3 \cdot \text{mol}^{-1}$ )	$\text{TCBT-3}^{\text{d}}$ $\text{PD}(V^E)$ (%)	$\sigma$ ( $\text{cm}^3 \cdot \text{mol}^{-1}$ )
288.15	5.51	0.0175	7.72	0.0233	hv <sup>g</sup>	hv	15.83	0.0552
293.15	5.32	0.0168	20.98	0.0645	hv	hv	27.62	0.0870
298.15	5.06	0.0162	20.67	0.0638	hv	hv	18.77	0.0642
303.15	4.87	0.0160	20.25	0.0632	hv	hv	12.47	0.0425
308.15	4.75	0.0162	19.49	0.0618	hv	hv	18.80	0.0722
313.15	4.84	0.0175	19.83	0.0639	hv	hv	19.17	0.0712
288.15–313.15 <sup>e</sup>	5.07	0.0186	2.62	0.0094	14.37	0.0506	11.75	0.0381
288.15–313.15 <sup>f</sup>	5.03	0.0167	31.72	0.1027	hv	hv	hv	hv

<sup>a</sup> Eqs. 6–12, 18;  $l_{ij} = 0$ <sup>b</sup> Eqs. 6–12, 18<sup>c</sup> Eqs. 6–16, 18;  $k_{ij} = l_{ij} = m_{ij} = 0$ ;  $\alpha_{ij} = 0.3$ <sup>d</sup> Eqs. 6–16, 18;  $l_{ij} = m_{ij} = 0$ ;  $\alpha_{ij} = 0.3$ <sup>e</sup> Prediction of  $V^E$  using temperature-independent parameters<sup>f</sup> Prediction of  $V^E$  using temperature-dependent parameters<sup>g</sup> hv—high value

**Table 9** Correlation of  $V^E$  for the 1-butanol (1) + chloroform (2) + benzene (3) ternary system

$T$ (K)	$\Delta g_{123}(J \cdot mol^{-1})$	$\Delta g_{213}(J \cdot mol^{-1})$	$\Delta g_{312}(J \cdot mol^{-1})$	$PD(V^E)$	$\sigma$
	$\Delta g_{132}(J \cdot mol^{-1})$	$\Delta g_{231}(J \cdot mol^{-1})$	$\Delta g_{321}(J \cdot mol^{-1})$	(%)	( $cm^3 \cdot mol^{-1}$ )
288.15					
TCBT-2 <sup>a</sup>	$0.242155 \times 10^4$	$-0.354164 \times 10^4$	$-0.100651 \times 10^4$	2.66	0.0111
	$-0.432052 \times 10^3$	$0.419419 \times 10^4$	$0.134159 \times 10^6$		
TCBT-3 <sup>b</sup>	$0.758883 \times 10^4$	$-0.940626 \times 10^3$	$-0.578481 \times 10^4$	1.67	0.0064
	$0.903925 \times 10^4$	$-0.422690 \times 10^2$	$-0.894742 \times 10^4$		
293.15					
TCBT-2	$0.243634 \times 10^4$	$-0.350073 \times 10^4$	$-0.102652 \times 10^4$	2.34	0.0094
	$-0.406890 \times 10^3$	$0.410023 \times 10^4$	$0.117706 \times 10^6$		
TCBT-3	$-0.341819 \times 10^4$	$0.130816 \times 10^3$	$-0.235320 \times 10^3$	1.60	0.0060
	$0.756450 \times 10^4$	$-0.313663 \times 10^4$	$0.649785 \times 10^4$		
298.15					
TCBT-2	$0.243936 \times 10^4$	$-0.340318 \times 10^4$	$-0.900287 \times 10^3$	2.00	0.0077
	$-0.478844 \times 10^3$	$0.395155 \times 10^4$	$0.986065 \times 10^5$		
TCBT-3	$0.726134 \times 10^4$	$-0.451356 \times 10^3$	$-0.575173 \times 10^4$	1.38	0.0044
	$0.809144 \times 10^4$	$-0.530041 \times 10^3$	$-0.837497 \times 10^4$		
303.15					
TCBT-2	$0.237066 \times 10^4$	$-0.305383 \times 10^4$	$-0.815095 \times 10^3$	1.76	0.0066
	$-0.492765 \times 10^3$	$0.363026 \times 10^4$	$-0.286823 \times 10^4$		
TCBT-3	$-0.397164 \times 10^4$	$-0.388234 \times 10^3$	$0.960691 \times 10^3$	1.16	0.0041
	$0.827809 \times 10^4$	$-0.341436 \times 10^4$	$0.724872 \times 10^4$		
308.15					
TCBT-2	$0.237568 \times 10^4$	$-0.306729 \times 10^4$	$-0.652608 \times 10^3$	1.64	0.0061
	$-0.610811 \times 10^3$	$0.360214 \times 10^4$	$-0.148557 \times 10^5$		
TCBT-3	$-0.429031 \times 10^4$	$-0.257027 \times 10^3$	$-0.250666 \times 10^3$	1.24	0.0042
	$0.961359 \times 10^4$	$-0.378274 \times 10^4$	$0.836248 \times 10^4$		
313.15					
TCBT-2	$0.246110 \times 10^4$	$-0.328388 \times 10^4$	$-0.470757 \times 10^3$	1.72	0.0066
	$-0.660702 \times 10^3$	$0.346506 \times 10^4$	$0.275323 \times 10^6$		
TCBT-3	$-0.447078 \times 10^4$	$-0.104401 \times 10^4$	$0.148843 \times 10^4$	1.38	0.0049
	$0.988870 \times 10^4$	$-0.380606 \times 10^4$	$0.874493 \times 10^4$		
288.15–313.15 <sup>c</sup>					
TCBT-2	$0.331960 \times 10^4$	$-0.259234 \times 10^4$	$-0.828002 \times 10^3$	8.14	0.0265
	$0.367322 \times 10^4$	$0.840441 \times 10^3$	$-0.591097 \times 10^4$		
TCBT-3	$0.115991 \times 10^4$	$-0.388894 \times 10^2$	$-0.692183 \times 10^3$	2.38	0.0083
	$-0.299962 \times 10^4$	$0.301905 \times 10^4$	$0.894278 \times 10^3$		
288.15–313.15 <sup>d</sup>					
TCBT-2	$0.266526 \times 10^4$	$-0.517119 \times 10^4$	$0.465144 \times 10^4$	2.87	0.0107
	$-0.290106 \times 10^4$	$0.464600 \times 10^4$	$0.128070 \times 10^6$		
TCBT-3	$0.209318 \times 10^4$	$0.196298 \times 10^4$	$-0.427686 \times 10^4$	4.00	0.0142
	$-0.110182 \times 10^4$	$0.379155 \times 10^4$	$-0.548159 \times 10^5$		

<sup>a</sup> Eqs. 6–18;  $k_{ij} = l_{ij} = m_{ij} = 0$ ;  $\alpha_{ij} = 0.3$ <sup>b</sup> Eqs. 6–18;  $l_{ij} = m_{ij} = 0$ ;  $\alpha_{ij} = 0.3$ <sup>c</sup> Correlation of  $V^E$  using temperature-independent binary parameters<sup>d</sup> Correlation of  $V^E$  using temperature-dependent binary parameters

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